

OKLAHOMA SCHOOL of SCIENCE and MATHEMATICS

22nd Annual OSSM Middle School Math: An Awesome Contest—Round Two

7th and 8th Grade Test B Spring 2024

Before you begin:

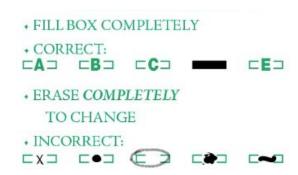
- 1. Please write your name on your answer sheet.
- 2. On your name tag you have been given a three-digit OSSM student ID number. On the answer sheet, in the lower right-hand corner, there is a place to fill in the three-digit student ID number (use the first three boxes, leaving the rest blank).
- 3. Fill in the appropriate bubbles for your OSSM student ID.

Directions:

Use the scratch paper provided to do your work.

Choose the appropriate answer, and then fill in the corresponding bubble
ON THE ANSWER SHEET.

DO NOT MAKE ANY STRAY MARKS ON YOUR ANSWER SHEET; it may cause the machine to misread your answer sheet and may disqualify your score.



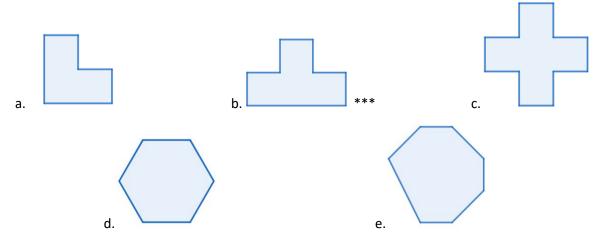
This is a 40-question, 1-hour contest. All questions are multiple-choice. Figures are not to scale. Each question is worth one point. Your score will be the number of correct answers. There is no partial credit or penalty for wrong answers. Please continue working or reworking problems until time is called.

Fill in your answers ON THE ANSWER SHEET by filling in the corresponding bubble.

DO NOT MAKE ANY STRAY MARKS ON YOUR ANSWER SHEET!

You may use this space for scratch paper.

- 1. 123 + 234 + 345 =
 - a. 602
 - b. 612
 - c. 692
 - d. 702 ***
 - e. 792
- 2. Which of the following shapes is an octagon?

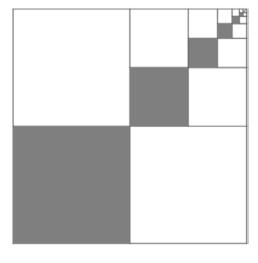


- 3. Which of these numbers is a square root of a square root of 1,600,000,000?
 - a. 200 ***
 - b. 400
 - c. 2,000
 - d. 4,000
 - e. 40,000
- 4. What is the slope of the line with equation -4x + 4y = 8?
 - a. -4
 - b. -2
 - c. -1
 - d. 1 ***
 - e. 2
- 5. Elijah has 108 M&Ms. He is willing to share with James, as long as James only takes whole M&Ms. Which fraction of Elijah's M&Ms can James **NOT** take?
 - a. 1/6
 - b. 1/8 ***
 - c. 1/9
 - d. 1/12
 - e. 1/27

	Vice President, one will be Treasurer, and one will be Project Manager. How many possible ways are there to assig one of the jobs to each woman?		
	a.	12	
	b.	16	
	C.	20	
	d.	24 ***	
	e.	28	
7.	The three	e angles of my triangle have degree-measures $3x^{\circ}$, $4x^{\circ}$, and $5x^{\circ}$. What is the value of x?	
	a.		
	b.	6	
		12	
		15 ***	
		18	
	C.		
8.	If I pour ou	t 8 cups of milk from my jug, I would have 3 cups less remaining in the jug than I would have if I had	
٥.	•	t half of the milk instead. How many cups of milk are in the jug before I pour anything out?	
	-	10 ***	
	b.	11	
	C.	11.5	
		12	
	e.	12.5	
۵	Mhat ic th	e greatest common factor of the numbers $12 imes 12$ and $4 imes 81$?	
Э.		24	
		36 ***	
	C.	48 54	
	_		
	e.	72	
10	The numer	ical value of the area of a square is exactly equal to the numerical value of its perimeter. What is the	
10.		rical value of the area of a square is exactly equal to the numerical value of its perimeter. What is the	
		ne side of the square?	
	a.	2 4 ***	
	b.		
	c.	6	
	d.		
	e.	10	
11	. About how much less time does a trip of 70 miles take if you travel 75 miles per hour than if you travel 70 miles per		
	hour?	That hess time does a trip of 70 times take if you travel 75 times per flour than if you travel 70 times per	
	a.	3 minutes	
	b.	3.5 minutes	
	C.	4 minutes ***	
	d.	4.5 minutes	
	e.	5 minutes	

6. Anna, Robin, Danny, and Sydney are starting a company together. One of them will be the President, one will be

- 12. Which of the following is **NOT** a whole number?
 - a. $\sqrt{4900}$
 - b. $\sqrt{6400}$
 - c. $\sqrt{9000}$ ***
 - d. $\sqrt{12100}$
 - e. $\sqrt{40000}$
- 13. In this figure, the large square is divided into four equal smaller squares. The lower left sub-square is shaded, and then the entire subdivision/shading process is repeated (to infinity!) inside the upper right sub-square. What fraction of the largest square is shaded?
 - a. 1/4
 - b. 8/27
 - c. 8/25
 - d. 1/3 ***
 - e. 5/12

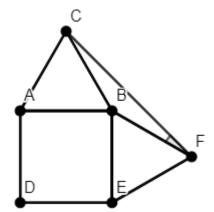


- 14. On the website scamazon.com, 15 yo-yos and 25 frisbees cost a total of \$600. What is the total cost of 21 yo-yos and 35 frisbees?
 - a. \$700
 - b. \$750
 - c. \$770
 - d. \$800
 - e. \$840 ***

15. If
$$\frac{1}{x} = -2$$
, then $\frac{1}{1+x^2} =$

- a. -1/3
- b. 1/5
- c. 2/3
- d. 4/5 ***
- e. 4/3
- 16. Evaluate $16^{-3/4}$.
 - a. -12
 - b. -8
 - c. 1/12
 - d. 1/8 ***
 - e. 12
- 17. *N* is the smallest two-digit number whose value is strictly less than twice the product of its digits. What is the <u>sum</u> of the digits of *N*?
 - a. 8
 - b. 9 ***

- c. 10
- d. 11
- e. 12
- 18. If the edge length of cube A is 10% of the edge length of cube B, then the volume of cube A is _____ of the volume of cube B.
 - a. 0.001 %
 - b. 0.01 %
 - c. 0.1 % ***
 - d. 1%
 - e. 10 %
- 19. Which, if any, is a true inequality?
 - a. $20 \times 24 < 6 \times 8 \times 10$
 - b. $20 \times 24 < 19 \times 25$
 - c. $20 \times 24 < 2 \times 120 + 12 \times 20$
 - d. $20 \times 24 < 3 \times 5 \times 5 \times 7$ ***
 - e. None of the above is a true inequality.
- 20. This diagram is made of a square (ABED), two equilateral triangles (ΔABC and ΔEBF), and an isosceles triangle (ΔBFC). What is the measure of ΔBFC ?
 - a. 5°
 - b. 10°
 - c. 12°
 - d. 15° ***
 - e. 20°



- 21. Evaluate $N \times N N \times N \times N$, if N = -2.
 - a. -12
 - b. -8
 - c. -4
 - d. 12 ***
 - e. 24
- 22. What is the sum of the first fifty odd positive whole numbers?
 - a. 2000
 - b. 2500 ***
 - c. 2525
 - d. 4900
 - e. 4950
- 23. The rule " $x \to -x$ " is an example of a rule that, if you apply it twice in a row, gives you back the same number you started with (since -(-x) = x). Which of the following rules also has the property that doing it twice in a row always gives you back the number you started with?
 - a. $x \rightarrow 2x$
 - b. $x \rightarrow 0$

c.
$$x \rightarrow |x|$$

d.
$$x \rightarrow 1 + x$$

e.
$$x \rightarrow 1 - x^{***}$$

$$24. \frac{\sqrt{2 \cdot 4 \cdot 6 \cdot 8 \cdot 10 \cdot 12}}{\sqrt{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \cdot 6}} =$$

a.
$$\sqrt{2}$$

c.
$$6\sqrt{2}$$

e.
$$6\sqrt{6}$$

25. A parallelogram in the xy-plane has vertices at (2,-1), (7,1), (1,4), and (-4,2). What are the coordinates of the point where its two diagonals intersect?

a.
$$\left(\frac{5}{4}, \frac{5}{4}\right)$$

b.
$$(\frac{5}{4}, \frac{7}{4})$$

b.
$$\left(\frac{5}{4}, \frac{7}{4}\right)$$

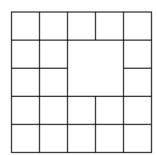
c. $\left(\frac{3}{2}, \frac{3}{2}\right) ****$
d. $\left(\frac{7}{4}, \frac{5}{4}\right)$

d.
$$\left(\frac{7}{4}, \frac{5}{4}\right)$$

$$e = \left(\frac{7}{4}, \frac{5}{4}\right)$$

26. One tablet of iodine makes 2 quarts of water drinkable. If you have 5 people who need one gallon of water each per day for 7 days, how many iodine tablets do you need? (4 quarts = 1 gallon).

27. How many squares appear in this figure?



28.
$$(\sqrt[16]{16}) \times (\sqrt[16]{16}) =$$

b.
$$\sqrt{2} ***$$

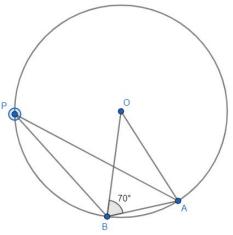
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e.	VΟ

- 29. If 2y x = z, then 2x + 2z =
 - a. -2y
 - b. 3*y*
 - c. -3y
 - d. 4y ***
 - e. -4y
- 30. A rectangle has area 300 cm² and perimeter 70 cm. Which of the following is the distance between two opposite corners of the rectangle?
 - a. 20 cm
 - b. 21 cm
 - c. 24 cm
 - d. 25 cm ***
 - e. 28 cm
- 31. The number 111—made by writing down 3 ones—is evenly divisible by 3 (because $111 = 3 \times 37$). Which of the following numbers is evenly divisible by 99?
 - a. The number made by writing down 9 ones
 - b. The number made by writing down 11 ones
 - c. The number made by writing down 18 ones ***
 - d. The number made by writing down 22 ones
 - e. The number made by writing down 99 ones
- 32. A container with a circular base has a height of 2 meters. A pole 6 meters long (but no longer) can be placed completely inside the container, resting at an angle. What is the volume of the tank?
 - a. $8\pi \text{ m}^3$
 - b. $12\pi \text{ m}^3$
 - c. $16\pi \text{ m}^3 ****$
 - d. $24\pi \text{ m}^3$
 - e. $32\pi \text{ m}^3$
- 33. The graph of the equation |y-1| = |y+1| in the xy-plane is, geometrically:
 - a. a horizontal line ***
 - b. a vertical line
 - c. a circle
 - d. a square
 - e. the empty set (the equation has no solutions in the xy-plane)

34. The circle shown is centered at O with points P, B, A along the circumference.

If $\angle OBA = 70^{\circ}$, what is the measure of $\angle BPA$?

- a. 20° ***
- b. 25°
- c. 30°
- d. 35°
- e. Not enough information.



- 35. How many different "words" of at least one letter can be made from the letters in OSSM? Your list should include words like M, MSS, SMS, and MOSS... but not MOOS, because there is only one O available to use in OSSM.
 - a. 32
 - b. 34 ***
 - c. 36
 - d. 38
 - e. 40

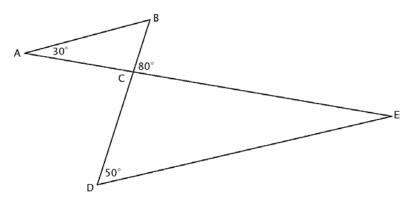
36. In the diagram, which of the following MUST BE TRUE?

a.
$$\angle ABC = \angle CED$$

b.
$$AB = CD$$

c.
$$DC^2 + CE^2 = DE^2$$

- d. \overline{AB} is parallel to \overline{DE} ***
- e. The area of ΔABC is one-fourth the area of ΔCDE

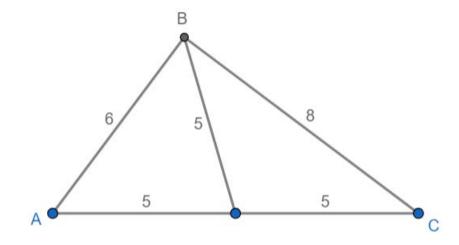


- 37. The length of a rectangle is increased by 10% and the width of the same rectangle is decreased by 10%. How does the area of the new rectangle compare to the original rectangle?
 - a. The area of the new rectangle is less than the area of the original rectangle. ***
 - b. The two rectangles have the exact same area.
 - c. The area of the new rectangle is greater than the area of the original rectangle.
 - d. No determination can be made unless the exact length and width of the original rectangle are given.

38. What is the area of $\triangle ABC$?



- b. 20
- c. 24 ***
- d. 25
- e. 30



- 39. In the time it takes Tajvir to knit twelve scarves, Yuehuan can knit fifteen scarves. If Tajvir starts knitting scarves at 8am, and Yuehuan starts at noon, then by 8pm Tajvir will have knitted exactly 1 more scarf than Yuehuan has. How long does it take Yuehuan to knit one scarf?
 - a. 1 hour, 30 minutes
 - b. 1 hour 36 minutes ***
 - c. 1 hour, 45 minutes
 - d. 1 hour, 48 minutes
 - e. 2 hours
- 40. Two equal circles, each of radius 2, are positioned so that each one passes through the other one's center. What is the area of the shaded region where they overlap?

a.
$$\frac{8\pi}{3} - 2\sqrt{3} ***$$

b.
$$\frac{8\pi}{3} - \sqrt{3}$$

c.
$$4 - \frac{\pi}{3}$$

d.
$$\frac{\pi}{3} + 2\sqrt{3}$$

b.
$$\frac{8\pi}{3} - \sqrt{3}$$

c. $4 - \frac{\pi}{3}$
d. $\frac{\pi}{3} + 2\sqrt{3}$
e. $\frac{2\pi}{3} + \sqrt{3}$

