

22nd Annual OSSM Middle School Math: An Awesome Contest—Round Two

6th Grade Test A

Spring 2024

Before you begin:

- 1. Please write your name on your answer sheet.
- On your name tag you have been given a three-digit OSSM student ID number. On the answer sheet, in the lower right-hand corner, there is a place to fill in the three-digit student ID number (use the first three boxes, leaving the rest blank).
- 3. Fill in the appropriate bubbles for your OSSM student ID.

Directions:

Use the scratch paper provided to do your work.

Choose the appropriate answer, and then fill in the corresponding bubble ON THE ANSWER SHEET. DO NOT MAKE ANY STRAY MARKS ON YOUR ANSWER SHEET; it may cause the machine to misread your answer sheet and may disqualify your score.

This is a 40-question, 1-hour contest. All questions are multiple-choice. Figures are not to scale. Each question is worth one point. Your score will be the number of correct answers. There is no partial credit or penalty for wrong answers. Please continue working or reworking problems until time is called.

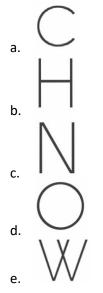
Do Not Open or Turn Over Until Instructed To Do So

Fill in your answers ON THE ANSWER SHEET by filling in the corresponding bubble.

DO NOT MAKE ANY STRAY MARKS ON YOUR ANSWER SHEET!

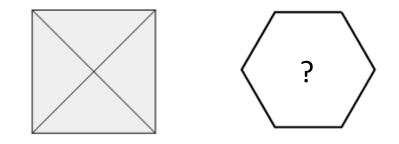
You may use this space for scratch paper.

- 1. What is the sum of the first ten odd numbers (beginning with the number 1)?
 - a. 50
 - b. 99
 - c. 100
 - d. 101
 - e. 110
- 2. Which of the following letters of the alphabet has <u>no</u> lines of symmetry?



- 3. What digit appears in the tens place of $5 \times 5 \times 5$?
 - a. 0
 - b. 1
 - c. 2
 - d. 4
 - e. 5
- 4. Elijah has 84 M&Ms. He is willing to share with James, as long as James only takes whole M&Ms. Which fraction of Elijah's M&Ms can James NOT take?
 - a. 1/2
 - b. 1/3
 - c. 1/6
 - d. 1/7
 - e. 1/8

- 5. Currently, a father is three times as old as his son. In 15 years, he will be twice as old as his son. What is the sum of the father's and son's ages now?
 - a. 50
 - b. 60
 - c. 70
 - d. 80
 - e. 90
- 6. Pictured here is a square with its two diagonals drawn. How many diagonals does a regular hexagon have?



- a. 7
- b. 8
- c. 9
- d. 10
- e. 12
- 7. If I pour out 5 cups of milk from my jug, I would have 2 cups less remaining in the jug than I would have if I had poured out half of the milk instead. How many cups of milk are in the jug before I pour anything out?
 - a. 1
 - b. 3
 - c. 5
 - d. 6
 - e. 14

8. If $30 \times N + 80 = 100$, then N =

- a. 1/3
- b. 2/3
- c. 6
- d. 10
- e. -10
- 9. In a right triangle, one of the acute angles is twice the measure of the other acute angle. What is the measure of the larger of the two acute angles?
 - a. 30 degrees
 - b. 45 degrees
 - c. 60 degrees
 - d. 70 degrees
 - e. 90 degrees

10. (-3)(-3) - (-3)(-3)(-3) =a. -36 b. -24 c. -18 d. 18

- e. 36
- 11. I start with zero rocks in my rock collection. On Day 1, I add 1 rock to my collection and then remove my least favorite rock (leaving me with zero rocks again). On Day 2, I add 2 rocks to my collection, and then remove my least favorite rock. The pattern continues: on Day *N*, I add *N* new rocks to my collection, then remove my least favorite rock. How many rocks will be in my collection at the end of Day 15?
 - a. 100
 - b. 105
 - c. 110
 - d. 115
 - e. 120
- 12. Pick a whole number. Multiply that number and the next higher number together, and look at the final digit of the result. (For example, $6 \times 7 = 42$ and the final digit is 2, or $10 \times 11 = 110$ and the final digit is 0.) What is the highest possible digit you can get this way?
 - a. 2
 - b. 4
 - c. 6
 - d. 8
 - e. 9

13. What is the remainder when you divide 1,450 by 7?

- a. 1
- b. 2
- c. 3
- d. 4
- e. 5
- 14. Starting on Monday, April 1, Joseph earns 50 cents every day, Monday through Friday, for doing weekday chores, as well as one dollar on Saturday for his Saturday chores, and one dollar on Sunday for Sunday chores. How much will Joseph earn for doing chores the whole month of April (30 days)?
 - a. \$16
 - b. \$17
 - c. \$18
 - d. \$19
 - e. \$20

15. Which of the following could **not** be the three side lengths of a triangle?

- a. 0.9, 1.5, 2.2
- b. 10, 400, 400
- c. $\sqrt{5}$, $\sqrt{6}$, $\sqrt{7}$
- d. 1, 2, π
- e. 1/4, 1/3, 1/2

16. Twice my number is less than half of my number. Which of the following must be true about my number?

- a. It is negative
- b. It is positive
- c. It is even
- d. It is odd
- e. It is zero

17. Which of the following is closest in value to 150% of 75?

- a. 100
- b. 110
- c. 120
- d. 130
- e. 140

18. Which, if any, is a true inequality?

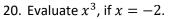
- a. 3 + 3 + 3 + 3 + 3 < 1 + 2 + 3 + 4 + 5
- b. 3 3 3 3 3 3 < 1 2 3 4 5
- c. $3 \times 3 \times 3 \times 3 \times 3 < 1 \times 2 \times 3 \times 4 \times 5$

d.
$$\left(\left((3\div3)\div3\right)\div3\right)\div3 < \left(\left((1\div2)\div3\right)\div4\right)\div5$$

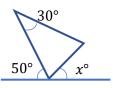
e. None of the above is a true inequality.

19. Consider the isosceles triangle shown whose two congruent sides enclose a 30° angle. What is the value of x?

- a. 30
- b. 50
- c. 55
- d. 75
- e. Not enough information.



- a. -8
- b. −6
- c. −4
- d. 6
- e. 8



21. How many two-digit numbers have digits that add up to a multiple of 9?

- a. 8
- b. 9
- c. 10
- d. 11
- e. 12

22. On a visit to the pet store, you notice that a goldfish and three guppies cost a total of \$12, while three goldfish and a guppy cost a total of \$8. What is the total cost to buy one goldfish and one guppy?

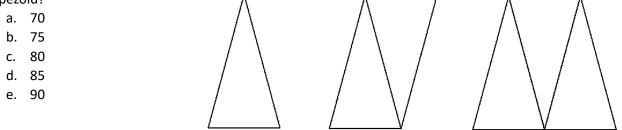
- a. \$1.50
- b. \$3.50
- c. \$4
- d. \$4.50
- e. \$5

23. How many different positive divisors does the number 210 have? (Both 1 and 210 count as divisors.)

- a. 12
- b. 14
- c. 16
- d. 18
- e. 20

24. $\sqrt{77 \times 21 \times 33} =$

- a. 229
- b. 231
- c. 237
- d. 239
- e. 241
- 25. Here are three shapes made out of copies of an isosceles triangle: the triangle itself, a parallelogram, and a trapezoid. The perimeter of the triangle is 50 and the perimeter of the parallelogram is 60. What is the perimeter of the trapezoid?



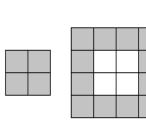
- 26. One tablet of iodine makes 1 quart of water drinkable. If you have 5 people who need one gallon of water each per day for 7 days, how many iodine tablets do you need? (4 quarts = 1 gallon).
 - a. 20
 - b. 28
 - c. 35
 - d. 70
 - e. 140

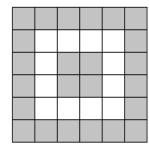
27. It has been estimated that there are as many as 4×10^{11} stars in the Milky Way galaxy. How many is that?

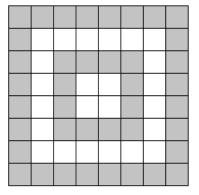
- a. 40 billion
- b. 400 billion
- c. 4 trillion
- d. 40 trillion
- e. 400 trillion
- 28. 8⁸ =
 - a. 2¹⁶
 - b. 2^{24}
 - c. 2³²
 - d. 2^{48}
 - e. 2⁶⁴

29. If $a \times b = 6$ and $a \times a = 3$, what is $b \times b$?

- a. 6
- b. 8
- c. 9
- d. 12
- e. 18
- 30. A pattern of four designs is shown below. The first design contains 4 small gray squares, the second design contains 12 small gray squares, the third design contains 24, and the fourth design contains 40. If <u>two more</u> designs were drawn to continue this pattern, how many small gray squares would be contained in the final, sixth design?







- a. 60
- b. 72
- c. 76
- d. 80
- e. 84

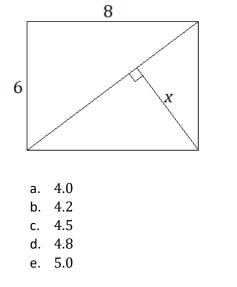
31. American coins are 1¢, 5¢, 10¢, or 25¢. How many different ways can I make 27 cents using American coins?

- a. 10
- b. 11
- c. 12
- d. 13
- e. 14

32. If you divide X by 80, you get a remainder of 45. If you divide X by 20, what is the remainder?

- a. 5
- b. 15
- c. 25
- d. 35
- e. 45
- 33. Assume that the statement "If a person is a student at the Oklahoma School of Science and Mathematics (OSSM), then the person must love the food served by the OSSM dining services" is true. Which, if any, of the following statements must also be true?
 - a. If a person loves the food served by the OSSM dining services, then the person must be an OSSM student.
 - b. If a person is <u>not</u> a student at OSSM, then the person does <u>not</u> love the food served by OSSM dining services.
 - c. If a person does <u>not</u> love the food served by OSSM dining services, then the person is <u>not</u> a student at OSSM.
 - d. All of the above statements are guaranteed to be true.
 - e. None of the above statements are guaranteed to be true.
- 34. Mia will either wear a dress, or she will wear jeans and a T-shirt. In her closet she has four dresses, two pairs of jeans, and six T-shirts. How many different outfits can she make?
 - a. 12
 - b. 16
 - c. 20
 - d. 32
 - e. 48
- 35. If tossing a fair icosahedron die (20 sides labeled with the numbers 1-20), what is the probability that you will roll a multiple of three or four?
 - a. $\frac{2}{5}$ b. $\frac{7}{20}$ c. $\frac{9}{20}$ d. $\frac{1}{2}$
 - e. $\frac{11}{11}$
 - e. <u>20</u>
 - 36. If the different letters in *OSSM* represent digits, then M + SSM + OSSM = 3552. (This equation represents adding together a 1-digit, 3-digit, and 4-digit number.) What is the value of O + S + S + M?
 - a. 10
 - b. 11
 - c. 15
 - d. 19
 - e. 20

37. What is the value of x in the rectangular figure below?



38. What is the value of the given expression?

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{2}}}$$

- a. 3/5
- b. 7/5
- c. 8/5
- d. 7/3
- e. 8/3
- 39. At the Intergalactic Party, there are three types of aliens: Woots, Yeets, and Zonks. There is at least one Woot who is taller than every Yeet, and there is at least one Zonk who is shorter than every Yeet. Which, if any, of the following statements (a-d) **CANNOT** possibly be true?
 - a. The shortest Woot is shorter than the shortest Zonk.
 - b. The shortest Zonk is shorter than the shortest Woot.
 - c. The shortest Woot is taller than the tallest Zonk.
 - d. The shortest Zonk is taller than the tallest Woot.
 - e. Each of the above statements could be true.

40. If A and B are positive whole numbers with A < B, then $A^B B^A =$

- a. (*AB*)^{*BA*}
- b. $(AB)^{A}A^{B-A}$
- c. $(AB)^B A^{B-A}$
- d. $(AB)^A B^{B-A}$
- e. $(AB)^B B^{B-A}$