## **Oklahoma School of Science and Mathematics**

## Fourteenth Annual Middle School Mathematics Contest 7<sup>th</sup> and 8<sup>th</sup> Grade Test, Round Two, Spring 2016



Directions: Write the answer to each question in the box to the right of the question. Units are given in plural form even if the singular form is correct. Use scratch paper to do your work. Calculators are allowed, but not necessary.

Common fractions should be in simplest form ( $\frac{a}{b}$ , not mixed numbers).

1.	. What is the next number in the sequence?						1.	$\frac{3}{8}$		
	$\frac{81}{64}, \frac{27}{32}, \frac{9}{16}, \dots$							8		
2.	If $k$ is parallel to $n$	$n$ , $\angle 2$ =	= 36° wł	nat is the	e measu	re of $\angle$	1?		2.	144°
	<u>k</u> 1	<b>→</b>								
	$\frac{m}{2}$	<b>→</b>								
3.	Solve the linear inequality for $x$ . $-2(x+1) < x+2$							3.	$x > \frac{-4}{3}$	
4.	If the given table o	f values	represe	nts point	ts on a s	traight l	ine, what v	vould the $y$ value be	4.	33
	when $x = 22$ ?		10	20	20	40	1			
		x	10	20	30	40	-			
		у	15	30	45	60				
5.		abet, for	what le	tter is th	ne ratio	of the le	tters befor	e it to the letters after it	5.	
	2:3?									a. <b>6</b> c. d.
	a.) J	b.) I	<	c.)	0	1	d.) P			
6.	A particular plant d	loubles i	its size e	very day	v. On Sa	turday i	t is <u>?</u> time	s as big as it was on the	6.	
	preceding Sunday.									a. b. c. <b>(d)</b> e.
	a.) 2	b.) 6	5	c.)	49	1	d.) 64	e.) 128		
7.	Which of the follow	ving is b	oth the	sum of t	wo prim	e numb	ers and the	product of two other	7.	
	prime numbers?									a. <b>(b)</b> c. d.
	a.) 19	b.) 2	21	c.)	31		d.) 51			
8.	. A particular basketball team scores an average of 67 points per game for the first four games,						8.			
	and an average of 64 points per game for the first five games. How many points did the team							a. <b>ⓑ</b> c. d. e.		
	score in its fifth gar	me?								
	a.) 51	b.) 5	52	c.)	53		d.) 54	e.) 55		
9.	A large equilateral	triangle	is made	of tesse	llated s	maller e	quilateral t	riangles that are 3	9.	
	inches on each side (see figure of a triangle made of 4 smaller triangles). How many of the							a. b. © d.		
	smaller triangles are necessary to build a triangle that is 12 inches on each side?									
	a.) 10	b.) 1	12	c.)	16		d.) 20	$\triangle$		

10. What is the value of	10. a. b. c. <b>(</b> )			
	b.) 30		d.) 150	a. b. c. w
11. $2^2 \times 3^3 \times 4^4 \times 6^6 \times 9$	9 =			11.
		c.) $2^{96} \times 3^{324}$	d.) $2^{12} \times 3^{24}$	a. (j). c. d.
12. Which of the followi	ng shapes could h	ave three consecu	tive sides of length 4, 4, and 10?	12.
a.) triangle	b.) rectangle	c.) trapezoid	d.) parallelogram e.) All of these	a. b. 🖒 d. e.
13. Two circles of area 1	13.			
rectangle (see figure	a. b. <table-cell> d.</table-cell>			
a.) 48 cm <sup>2</sup>	b.) 96 cm <sup>2</sup>	c.) 128 cm <sup>2</sup>	d.) 512 cm <sup>2</sup>	
14. An OSSM Calculus cl	ass increased in si	ze by $33.\overline{3}\%$ from	last semester to this semester. If	14.
the average number class last semester?	of students in the	Calculus class is 2	1, how many students were in the	a. 🐧. c. d. e.
a.) 15	b.) 18	c.) 21	d.) 24 e.) 28	
15. I'm thinking of a nat	ural number. If I s	quare my number	and divide by four, the quotient is	15.
16. What is my num	ber?			a. b. 🕝. d.
a.) 1	b.) 2	c.) 8	d.) 16	
16. For the given group	16.			
greatest. {1,	2, 2, 4, 5, 6, 9, 10}			a. b. c. 🗇
a.) median <me< td=""><td>an<mode< td=""><td>b.) mode<mear< td=""><td>n<median< td=""><td></td></median<></td></mear<></td></mode<></td></me<>	an <mode< td=""><td>b.) mode<mear< td=""><td>n<median< td=""><td></td></median<></td></mear<></td></mode<>	b.) mode <mear< td=""><td>n<median< td=""><td></td></median<></td></mear<>	n <median< td=""><td></td></median<>	
c.) median <mo< td=""><td></td><td>.,</td><td></td><td></td></mo<>		.,		
17. What is the value of	the given quotien	t? $\frac{4-2\times 6\div 3+}{}$	<u>1</u>	17.
		$2(3^2-2)+1$		a. <b>⑥</b> c. d.
a.) 0	b.) 1/15	c.) 1/3	d.) 9/2	
18. The sum of four nun	nbers is one-fourth	n. What is the aver	rage?	18.
a.) one-sixteen	thb.) one-fourth	c.) one-half	d.) 1	a b. c. d.
19. I have quarters and	19.			
quarters do I have?				a. (b. c. d.
a.) 1 quarters	b.) 5 quarters	c.) 7 quarters	d.) 13 quarter	
20. The roof of my hous	20.			
sides are 16 and 32,	then what is the p	erimeter of the tri	angle?	a. b. 🖒 d.
a.) 64	b.) 75.71	c.) 80	d.) 83.77	
21. If I add the digits of	my school ID and g	get 37, then my sch	nool ID cannot have ? numbers.	21.
a.) 4	b.) 5	c.) 6	d.) 38	⑤ b. c. d.

22. $x$ is a number between -4 and -3. Which is the smallest?	22.
a.) $x$ b.) $x-2$ c.) $x+2$ d.) $\frac{x}{2}$ e.) $3x$	a. b. c. d. @
23. Multiplying 5 by 20% gets the same results as dividing 5 by	23.
a.) 0.2 b.) 5 c.) 30 d.) 100	a. (b). c. d.
24. The number $\left(0.01\right)^{20}$ is equal to	24.
a.) $\frac{1}{10^{20}}$ b.) $\frac{1}{100^{40}}$ c.) $1 \times 10^{-20}$ d.) $100^{-20}$ e.) All of these	a. b. c. <b>(</b> ) e.
25. A perimeter of a rectangle is 38 inches, and the area of the rectangle is 54.25 square inches.	25.
What are the dimensions of the rectangle?	a. b. c. @. e.
a.) 5x14 inches b.) 4.5 x 14.5 inches c.) 4 x 15 inches	
d.) 3.5 x 15.5 inches e.) 7x7.75 inches	
26. A magazine price was reduced from 2014 price by 20% for 2015, but increased from the 2015	26.
price by 10% for 2016. If the price of the magazine is \$22/year for 2016, what was it for	a. b. c. 🕥
2014?	
a.) \$23.76 b.) \$24 c.) \$24.20 d.) \$25	
27. 20 math books weigh the same as 16 science books, then how many math books weigh the	27.
same as 20 science books?	a. b. c. 🐧
a.) 16 b.) 18 c.) 24 d.) 25	
28. If $x = -2$ , and $y = \frac{1}{4}$ , then what is the value of the expression $x^2 - 2xy + 24y^2$ ?	28. 6.5 or $\frac{13}{2}$
29. The Twilight saga is 608 minutes total for all of the movies. If you began watching it at 6:00	29. 4:08 am
p.m. on Friday, at what time (indicate a.m./p.m.) on what day would you finish if you never	Saturday
stopped?	
30. A student has 7 quizzes that average 91% exactly. The teacher decided to count one of these	30. 83%
quizzes twice, making the average go down to 90%. What was the score of the quiz that was	
counted twice?	
31. Combine the following into a single expression of the form $a\sqrt{b}$ .	31. <i>−</i> 4√7
$\sqrt{7} - \sqrt{28} - \sqrt{63}$	
32. Simplify the rational expression: $\frac{(x-2)(x^2-x-6)}{(3x^2-12)(x-3)}$	32. $\frac{1}{3}$
33. How many numbers are there between 25 and 125 that are multiples of 2 or 3 but not both?	33. 67
34. Express as a simple fraction: $0.\overline{3} + 0.\overline{17}$	34. $\frac{50}{99}$

35. Factor: $(3x^2 - 2xy - 8y^2)$	35. $(3x+4y)(x-2y)$
36. Find a quadratic equation with lead coefficient 1 in the form $ax^2 + bx + c = 0$ whose	$36. \ x^2 + 3x - 5 = 0$
solutions are $x = \frac{-3 \pm \sqrt{29}}{2}$	
37. Find the sum of all possible values of the digit $n$ such that the 5-digit number $219n5$ is	37. 12
divisible by 15	
38. Assuming $x$ and $y$ are positive, simplify the expression so that it is a simplified fraction with only positive integer exponents. $\left(\frac{4x^2}{9y^2}\right)^{-\frac{3}{2}}$	38. $\frac{27y^3}{8x^3}$
39. Of the 80 students in a class, one-fifth of them prefer orange soda, one-fourth prefer lemon-	39. 99°
lime soda. Half of what remain prefer cola, and the other half prefer root-beer. (Dr. Pepper	
was not an option.) If making a pie-chart, how many degrees should be given to cola?	
40. For what value of $x$ will the solution of the following equation be $y = 3x$ ? $4x + y = 3(1+x)$	40. $\frac{3}{4}$ or 0.75
41. If $x \Im y = 2x - y^2$ , then $3 \Im (5 \Im 4) = ?$	4130
42. What is the positive difference between the sum of the 6 smallest prime numbers and the	42. 4
sum of the three largest composite number less than 17?	
43. $1024 = 2^{10}$ . 1 terabyte is 1024 gigabytes. 1 gigabyte is 1024 megabytes. 1 megabyte is 1024	<b>43</b> . 2 <sup>43</sup>
kilobytes. 1 kilobyte is 1024 bytes. 1 byte is 8 bits. How many bits in a terabyte? Write the	
answer in the form $2^n$ .	
44. What is the smallest difference between factors of 2016?	44. 6
(example: 672x3=2016, 672-3=669)	
45. There are 216 stitches on a regulation baseball. If I can stitch 4 stitches in 25 seconds, how	45.
long will it take to stitch a baseball? Write the answer in minutes and seconds.	22 mins 30 secs
46. The sum of two natural numbers is 96. Their difference is 16. What is the smaller number?	46. 40
47. Three fair dice are thrown. What is the probability that the product of the three numbers is a	47. 91
multiple of 5? Write the answer as a reduced fraction.	$\frac{47.}{216}$
48. Consider the shape illustrated below made of a square (4 meter on a side) and a right triangle	48. 24 meters
(3 meter base). What is the minimum amount of fence needed to build a pen as illustrated?  4 m  3 m	
49. What is the sum of all factors of the number 2016? (Including 1 and itself).	49. 6552
50. 2016 has only 2, 3, and 7 as prime factors. What are the next three numbers to have only	50. 2058, 2268,
these same three prime factors?	2352